## 國立台灣大學九十二學年度碩士班招生考試試題

科目:物理化學(A)-甲

題號: 73

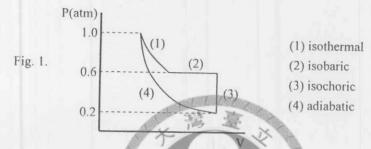
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※注意:作答時,請於答案卷上標明作答之部分及其題號。

## Part I 與 Part II 需分開作答

Part I:

1. One mole of an ideal gas ( $C_v = 3R/2$ ), initially at 1.0 atm and 300 K, undergoes a reversible cycle containing four steps as shown in Fig. 1.



Find  $\Delta U$ ,  $\Delta S$ , and the work done for each step.

- 2. An electrochemical proton gradient is used to synthesize ATP in mitochondria. The pH inside the mitochondria membrane is 1.5 units lower than outside and the inside potential is -0.2 V relative to the outside. Inside the mitochondria,  $[P_i] = [ADP] = [ATP] = 1$  mM.  $T = 37^{\circ}$ C.
- (a) How much free energy is required to synthesize 1 mol of ATP inside the mitochondria (via the reaction: ADP +  $P_i \rightarrow$  ATP)? Assume that all the activity coefficients are 1. Is the process spontaneous?
- (b) How much free energy is released by moving 1 mol of proton from the outside to the inside?
- (c) If all the free energy from proton transport is used to synthesize ATP, how may protons have to be transported to synthesize 1 molecule of ATP?
- 3. A system has the following energy levels ( $\epsilon_i$ ) and degeneracies ( $g_i$ ): 10%  $\epsilon_i/k$  0 150 K 300 K  $g_i$  1 2 3  $\exp\left(-\epsilon_i/kT\right)$  1 0.606 0.368 at 300 K

Where, k is the Boltzmann constant.

- (a) Calculate the partition function of the system at 300 K.
- (b) Calculate the fractional population of each energy level at 300 K.
- (c) Calculate the entropy of the system at 300 K.

## Part II

- 1. This problem concerns the molecular orbitals of benzene
  - (a) Write down the orbital energy levels for the  $\pi$  orbitals and fill with electrons
  - (b) Write down the molecular orbital for the lowest and the highest orbitals
  - (c) Explain the stability of benzene

(12%)

- 2. The observed rate law for the reaction  $2 O_3 \rightarrow 3 O_2$  is: Rate = k  $[O_3]^2/[O_2]$ . Propose a mechanism for the reaction. (1) %)
- 3 Mathematical problems:
  - (a) Two fair dice (骰子) are rolled. What is the probability that at least one of them shows a "3".
  - (b) Five coins are tossed. What is the probability that the number of heads(王) exceeds the number of tails(反)?
  - (c) Please integrate the function  $f(x) = \exp(-3x)$  from 0 to infinity (12%)
- 4. Explain:
  - (a) SF<sub>6</sub> can be made but SCI<sub>6</sub> cannot
  - (b) The molecular orbital of Li2
  - (c) Franck-Condon Principle

(15%)