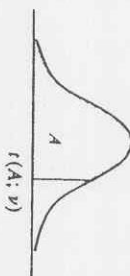


1. (a) Explain the mean ($\bar{X}$), the median (Me) and the mode (Mo). (5%)
 (b) What would be an appropriate density function for a distribution where $\bar{X} = \text{Me} = \text{Mo}$, and why? (5%)
2. (a) The mean length of all possible fish in a tank is 31.7 cm and the variance is 4.8. A biologist is requested to catch two of these fish measuring 35 and 37 cm and bring them over to the lab for further study. What is the probability that he will find such animals in the tank? (10%)
 (b) After long hours and many mosquito bites, our poor biologist in problem (a) returned to the lab complaining no such fish existed in the tank. He collected the following length data: 27.5, 28.3, 30.8, 31.3, 32.4, and 33.8. Do you agree with him and why? (10%)
3. The slope of a linear regression is 2.7, the sum of products is 27.0 and the sum of squared deviation of Y's is 82.8. Are variables X and Y highly correlated and why? (10%)
4. What are the assumptions for analysis of variance (ANOVA)? If the assumptions are not met, what need to be done before ANOVA? If the assumptions obviously cannot be met, what can you do? (20%)
5. The von Bertalanffy growth equation (VBGE) $L_t = L_\infty(1 - e^{-k(t-t_0)})$ has been most commonly used to express the growth of marine species. If you conducted an age and growth study of redfish, and got two VBGE for males and females. How do you know if there is growth difference between males and females? (i.e. what kind of statistical test do you suggest and how?) (20%)
6. A fishery scientist went to several fish markets to collect weight (W) and length (L) data for dolphin fish and set up the weight-length relationship of dolphin fish for each area (fish market) following the equation $W = aL^b$. The scientist wish to know if the W-L relationship differs among areas, what kind of statistical test do you suggest and how? (20%)

TABLE 1. Percentiles of the t Distribution

Entry is $t(A; \nu)$ where $P\{t(\nu) \leq t(A; \nu)\} = A$



ν	A					
	.60	.70	.80	.85	.90	.95
1	0.325	0.727	1.376	1.963	3.078	6.314
2	0.289	0.617	1.061	1.386	1.886	2.920
3	0.277	0.584	0.978	1.250	1.638	2.353
4	0.271	0.569	0.941	1.190	1.533	2.132
5	0.267	0.559	0.920	1.156	1.476	2.015
6	0.265	0.553	0.906	1.134	1.440	1.943
7	0.263	0.549	0.896	1.119	1.415	1.895
8	0.262	0.546	0.889	1.108	1.397	1.860
9	0.261	0.543	0.883	1.100	1.383	1.833
10	0.260	0.542	0.879	1.093	1.372	1.812
11	0.260	0.540	0.876	1.088	1.363	1.796
12	0.259	0.539	0.873	1.083	1.356	1.782
13	0.259	0.537	0.870	1.079	1.350	1.771
14	0.258	0.537	0.868	1.076	1.345	1.761
15	0.258	0.536	0.866	1.074	1.341	1.753
16	0.258	0.535	0.865	1.071	1.337	1.746
17	0.257	0.534	0.863	1.069	1.333	1.740
18	0.257	0.534	0.862	1.067	1.330	1.734
19	0.257	0.533	0.861	1.066	1.328	1.729
20	0.257	0.533	0.860	1.064	1.325	1.725
21	0.257	0.532	0.859	1.063	1.323	1.721
22	0.256	0.532	0.858	1.061	1.321	1.717
23	0.256	0.532	0.858	1.060	1.319	1.714
24	0.256	0.531	0.857	1.059	1.318	1.711
25	0.256	0.531	0.856	1.058	1.316	1.708
26	0.256	0.531	0.856	1.058	1.315	1.706
27	0.256	0.531	0.855	1.057	1.314	1.703
28	0.256	0.530	0.855	1.056	1.313	1.701
29	0.256	0.530	0.854	1.055	1.311	1.699
30	0.256	0.530	0.854	1.055	1.310	1.697
40	0.255	0.529	0.851	1.050	1.303	1.684
60	0.254	0.527	0.848	1.045	1.296	1.671
120	0.254	0.526	0.845	1.041	1.289	1.658
∞	0.253	0.524	0.842	1.036	1.282	1.645

TABLE 1. (continued) Percentiles of the t Distribution

ν	A					
	.98	.985	.99	.9925	.995	.9975
1	15.895	21.205	31.821	42.434	63.657	127.322
2	4.849	5.643	6.965	8.073	9.925	14.089
3	3.482	3.896	4.541	5.047	5.841	7.453
4	2.999	3.298	3.747	4.088	4.604	5.598
5	2.757	3.003	3.365	3.634	4.032	4.773
6	2.612	2.829	3.143	3.372	3.707	4.317
7	2.517	2.715	2.998	3.203	3.499	4.029
8	2.449	2.634	2.896	3.085	3.355	3.833
9	2.398	2.574	2.821	2.998	3.250	3.690
10	2.359	2.527	2.764	2.932	3.169	3.581
11	2.328	2.491	2.718	2.879	3.106	3.497
12	2.303	2.461	2.681	2.836	3.055	3.428
13	2.282	2.436	2.650	2.801	3.012	3.372
14	2.264	2.415	2.624	2.771	2.977	3.326
15	2.249	2.397	2.602	2.746	2.947	3.286
16	2.235	2.382	2.583	2.724	2.921	3.252
17	2.224	2.368	2.567	2.706	2.898	3.222
18	2.214	2.356	2.552	2.689	2.878	3.197
19	2.205	2.346	2.539	2.674	2.861	3.174
20	2.197	2.336	2.528	2.661	2.845	3.153
21	2.189	2.328	2.518	2.649	2.831	3.135
22	2.183	2.320	2.508	2.639	2.819	3.119
23	2.177	2.313	2.500	2.629	2.807	3.104
24	2.172	2.307	2.492	2.620	2.797	3.091
25	2.167	2.301	2.485	2.612	2.787	3.078
26	2.162	2.296	2.479	2.605	2.779	3.067
27	2.158	2.291	2.473	2.598	2.771	3.057
28	2.154	2.286	2.467	2.592	2.763	3.047
29	2.150	2.282	2.462	2.586	2.756	3.038
30	2.147	2.278	2.457	2.581	2.750	3.030
40	2.123	2.250	2.423	2.542	2.704	2.971
60	2.099	2.223	2.390	2.504	2.660	2.915
120	2.076	2.196	2.358	2.468	2.617	2.860
∞	2.054	2.170	2.326	2.432	2.576	2.807

TABLE 2. Percentiles of the χ^2 DistributionEntry is $\chi^2(A; \nu)$ where $P(\chi^2(\nu) \leq \chi^2(A; \nu)) = A$ 

ν	.005	.010	.025	.050	.100	.900	.950	.975	.990	.995
1	0.00393	0.0157	0.00982	0.0393	0.0158	2.71	3.84	5.02	6.63	7.88
2	0.0100	0.0201	0.0506	0.103	0.211	4.61	5.99	7.38	9.21	10.60
3	0.072	0.115	0.216	0.352	0.584	6.25	7.81	9.35	11.34	12.84
4	0.207	0.297	0.484	0.711	1.064	7.78	9.49	11.14	13.28	14.86
5	0.412	0.554	0.831	1.145	1.61	9.24	11.07	12.83	15.09	16.75
6	0.676	0.872	1.24	1.64	2.20	10.64	12.59	14.45	16.81	18.55
7	0.989	1.24	1.69	2.17	2.83	12.02	14.07	16.01	18.48	20.28
8	1.34	1.65	2.18	2.73	3.49	13.36	15.51	17.53	20.09	21.96
9	1.73	2.09	2.70	3.33	4.17	14.68	16.92	19.02	21.67	23.59
10	2.16	2.56	3.25	3.94	4.87	15.99	18.31	20.48	23.21	25.19
11	2.60	3.05	3.82	4.57	5.58	17.28	19.68	21.92	24.73	26.76
12	3.07	3.57	4.40	5.23	6.30	18.58	21.03	23.34	26.22	28.30
13	3.57	4.11	5.01	5.89	7.04	19.81	22.36	24.74	27.69	29.82
14	4.07	4.66	5.63	6.57	7.79	21.06	23.68	26.12	29.14	31.32
15	4.60	5.23	6.26	7.26	8.55	22.31	25.00	27.49	30.58	32.80
16	5.14	5.81	6.91	7.96	9.31	23.54	26.30	28.85	32.00	34.27
17	5.70	6.41	7.56	8.67	10.09	24.77	27.59	30.19	33.41	35.72
18	6.26	7.01	8.23	9.39	10.86	25.99	28.87	31.53	34.81	37.16
19	6.84	7.63	8.91	10.12	11.65	27.20	30.14	32.85	36.19	38.58
20	7.43	8.26	9.59	10.85	12.44	28.41	31.41	34.17	37.57	40.00
21	8.03	8.90	10.28	11.59	13.24	29.62	32.67	35.48	38.93	41.40
22	8.64	9.54	10.98	12.34	14.04	30.81	33.92	36.78	40.29	42.80
23	9.26	10.20	11.69	13.09	14.85	32.01	35.17	38.08	41.64	44.18
24	9.89	10.86	12.40	13.85	15.66	33.20	36.42	39.36	42.98	45.56
25	10.52	11.52	13.12	14.61	16.47	34.38	37.65	40.65	44.31	46.93
26	11.16	12.20	13.84	15.38	17.29	35.56	38.89	41.92	45.64	48.29
27	11.81	12.88	14.57	16.15	18.11	36.74	40.11	43.19	46.96	49.64
28	12.46	13.56	15.31	16.93	18.94	37.92	41.34	44.46	48.28	50.99
29	13.12	14.26	16.05	17.71	19.77	39.09	42.56	45.72	49.59	52.34
30	13.79	14.95	16.79	18.49	20.60	40.26	43.77	46.98	50.89	53.67
40	20.71	22.16	24.43	26.51	29.05	51.81	55.76	59.34	63.69	66.77
50	27.99	29.71	32.36	34.76	37.69	63.17	67.50	71.42	76.15	79.49
60	35.53	37.48	40.48	43.19	46.46	74.40	79.08	83.30	88.38	91.95
70	43.28	45.44	48.76	51.74	55.33	85.53	90.53	95.02	100.4	104.2
80	51.17	53.54	57.15	60.39	64.28	96.58	101.9	106.6	112.3	116.3
90	59.20	61.75	65.65	69.13	73.29	107.6	113.1	118.1	124.1	128.3
100	67.33	70.06	74.22	77.93	82.36	118.5	124.3	129.6	135.8	140.2

Source: Reprinted, with permission, from C. M. Thompson, "Table of Percentage Points of the Chi-Square Distribution," *Biometrika* 32 (1941), pp. 188-89.