

1. Let  $X$  and  $Y$  be independent random variables each having the normal density  $N(0, \sigma^2)$ . Find the density of  $Z_1 = X + Y$  and  $Z_2 = X^2 + Y^2$ . (正確給 20 分)
2. Suppose the times of successive failures of a machine form a Poisson process on  $[0, \infty)$  with parameter  $\lambda$ . What is the probability of at least one failure during the time period  $(t, t+h)$ ,  $h > 0$ ? (正確給 20 分)
3. Based on a random sample of size  $n$ , find the maximum likelihood estimator of  $p$  for the geometric density:  $f(x|p) = p(1-p)^x$ ,  $x = 0, 1, 2, \dots$  (正確給 20 分)
4. The following data give the velocity ( $y$ ) of a river in feet per second corresponding to various depths expressed in terms of the ratio ( $x$ ) of the measured depth to the depth of the river. Use least squares to fit a parabola  $y = a + bx + cx^2$  to these points, choosing  $x - 0.4$  rather than  $x$  as the independent variable. (正確給 20 分)
 

$x$	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8
$y$	3.20	3.23	3.25	3.26	3.25	3.23	3.18	3.13	3.06

5. Why do we utilize a  $F$ -distribution for the decision in an analysis of variances (ANOVA)? What situations in a hypothesis test could utilize the method of ANOVA? (正確給 20 分)

試題隨卷繳回