

1. A sample of air occupies 1.0 L at 25°C and 1.00 atm. What pressure is needed to compress it to 100 cm³ at this temperature? (10%)
2. Show that $(\partial p / \partial T)_V = \alpha / \beta$, where $\alpha = 1/V(\partial V / \partial T)_p$ is the coefficient of thermal expansion and $\beta = -1/V(\partial V / \partial p)_T$ is the isothermal compressibility. (15%)
3. Calculate the entropy change of a sample of perfect gas when it expands isothermally from a volume V_i to a volume V_f . (15%)
4. The molar Gibbs energy of a certain gas is given by

$$G_m = RT \ln p + A + Bp + \frac{1}{2} Cp^2 + \frac{1}{3} Dp^3 \quad (15\%)$$
 where A, B, C, and D are constants. Obtain the equation of state of the gas.
5. Find the expression for the fugacity coefficient of a gas that obeys the equation of state

$$\frac{pV_m}{RT} = 1 + \frac{B}{V_m} + \frac{C}{V_m^2} \quad (15\%)$$
 where the fugacity coefficient of a gas is given by

$$\ln \phi = \int_0^p \left(\frac{Z-1}{p} \right) dp$$
 where Z is the compression factor of the gas.
6. Please derive the Gibbs-Duhem equation for a two-component mixture as follows

$$n_A d\mu_A + n_B d\mu_B = 0 \quad (15\%)$$
7. Show that two phases are in thermal equilibrium only if their temperatures are the same. (15%)