科目:統計學(B)

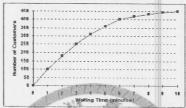
題號:407

共 8 頁之第 / 頁

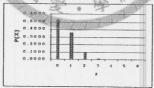
本份統計考題總分爲 100 分,總共分爲是非題、單選題與簡答題三大部份。

一、是非題(共 20 分, 每題 2 分): 請按照題號順序作答

- 1. Abel Alonzo, Director of Human Resources, is exploring the causes of employee absenteeism at Batesville Bottling during the last operating year (January 1, 1999 through December 31, 1999). The average number of absences per employee, computed from the personnel data of all employees, is a statistic.
- How many inventories do Christmas tree sales lots keep? A researcher goes from location to location around the city counting the number of trees in each lot. These numbers most likely represent ratio level of data.
- 3. The staff of Mr. Wayne Wertz, VP of Operations at Portland Peoples Bank, prepared a cumulative frequency ogive of waiting time for walk-in customers. The percentage of walk-in customers waiting one minute or less was 22%.



- 4. In its Industry Norms and Key Business Ratios, Dun & Bradstreet reported that Q1, Q2, and Q3 for 577 motorcycle dealers' current ratios were 1.3, 1.6 and 2.9, respectively. From this we can conclude that 68% of these dealers had current ratios between 1.3 and 2.9.
- 5. Let A be the event that a student is enrolled in an accounting course, and let S be the event that a student is enrolled in a statistics course. It is known that 30% of all students are enrolled in an accounting course and 40% of all students are enrolled in statistics. Included in these numbers are 15% who are enrolled in both statistics and accounting. From this information, it can be concluded that A and S are mutually exclusive.
- 6. The following graph is a binomial distribution with n = 6. This graph reveals that p < 0.5.



- 7. The average time between phone calls is 30 seconds. Assuming that the time between calls is exponentially distributed, the probability that more than a minute elapses between calls is 0.368.
- 8. Financial analyst Larry Potts needs a sample of 100 securities listed on either the New York Stock Exchange (NYSE) or the American Stock Exchange (AMEX). According to the Wall Street Journal's "Stock Market Data Bank," 2,531 NYSE securities and AMEX 746 securities were traded on the previous business day. Larry directs his staff to randomly select 77 NYSE and 23 AMEX securities. His sample is a proportionate stratified sample.
- 9. A bank officer wishes to estimate the amount of the average total deposits per customer at the bank. She wishes the estimate to be within \$200 of the actual average with 95% confidence. She assumes the standard deviation for this should be \$1000. The sample size should be at least 96.
- 10. You wish to determine the proportion of all secretaries who are familiar with a particular word processing package. You will conduct a random survey. The sample size should be at least 277 if you want to be 95% confident of the results and within 0.05 of the true population proportion.
- 二、單選題(共60分,每題3分):請按照題號順序作答
- 1. The United States Postal Service (USPS) offers a service called Priority Mail that promises 2-day delivery. It costs about \$3.00 to send a letter by Priority Mail within the United States. A spoken person for the USPS claims that it has a success rate of more than 95% in delivering letters within 2-day

### 科目:統計學(B)

題號:407

共 8 頁之第 2 頁

deadline. An experiment was conducted by sending letters from New York City to Cleveland, Ohio: 275 through priority mail and 378 through ordinary mail. The result was that 97.14% of the priority mails and 91.01% of the ordinary mails arrived on time. At 95% confidence level, which of the following conclusions is correct?

- A. Reject the null hypothesis. The spokesperson's claim is true.
- B. Don't reject the null hypothesis. The spokesperson's claim is not true.
- C. Reject the null hypothesis. The spokesperson's claim is not true.
- D. Don't reject the null hypothesis. The spokesperson's claim is true.
- E. None of above
- 2. Continue from the above example and given the following excel output. Which of the following conclusions is correct?

Test of Hypothesis About P1-P2

Test of P1-P2 = 0 Vs P1-P2 greater than 0 Priority Mail proportion (P1) = 0.9714Ordinary Mail proportion (P2) = 0.9101Test Statistic = 3.018 P-Value = 0.0013

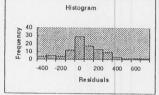
- A. At  $\alpha = 1\%$ , Do not reject the null hypothesis.
- B. There is no evidence to infer that Priority Mail delivers letters within two days more frequently than does ordinary mail at 95% confidence level.
- C. At  $\alpha = 5\%$ , reject the null hypothesis.
- D. There is significant evidence to infer that Priority Mail delivers letters within two days more frequently than does ordinary mail at 99% confidence level.
- E. None of above

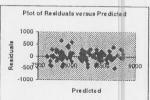
Questions 3 through 7 are based on the following information:

In an effort to explain to customers why their electricity bills have been so high lately, and how, specifically, they could save money by reducing the thermostat settings on both space heaters and water heaters, an electric utility company has collected total kilowatt consumption figures for last year's winter months, as well as thermostat settings on space and water heaters, for 100 homes.

Regression Statistics

| ANOVA      | R<br>A c<br>S t | ultiple R<br>Square<br>Ijusted R<br>andard Er<br>oservation | ror          | F 00          | .8415<br>.7081<br>.7021<br>213.7<br>100 |        |
|------------|-----------------|---|--------------|---------------|---|--------|
|            | df              | SS  | MS           | F             | Significan                              | ce F   |
| Regression | 2               | 10744454  | 5372227      | 117.64        | The second second                       | 0.0000 |
| Residual   | 97              | 4429664   | 45667        |               |   |        |
| Total      | 99              | 15174118  |              |               |   |        |
|            | Coefficients    | Standard<br>Error   | t Stat       | P-value       |   |        |
| Intercept  | 576.8           | 514.0   | 1.12         | 0.2646        |   |        |
| Space      | 90.61           | 6.48  | 13.99        | 0.0000        |   |        |
| Water      | 9.66            | 2.41  | 4.00         | 0.0001        |   |        |
| Histogr    | am              |   | of Residuals | versus Predic | led                                     |        |





|       | Coefficient | of    |
|-------|-------------|-------|
|       | Correlation | 1     |
|       | Space       | Water |
| Space | 1           |       |
| Water | 0.1578      | 1     |

- 3. Which of the following statement is correct?
  - A. The regression equation is  $\hat{y} = 576.8 + 90.61$ Space + 9.66 Water
  - B. The standard error of estimate is = 213.7.
  - C. 70.81% of the variation in sales is explained by the model.

科目:統計學(B)

題號:

共 8 頁之第 子

- D. The model fits reasonably well.
- E. All of the above.
- 4. Test the validity of the model.
  - A. Since F = 117.64, there is no evidence to conclude that the model is valid.
  - B. Since p-value = 0, there is no evidence to conclude that the model is valid.
  - C. At  $\alpha = 5\%$ , there is enough evidence to conclude that the model is valid.
  - D. Since  $R^2 = .7081$ , there is no evidence to conclude that the model is valid.
  - E. None of the above.
- 5. About the coefficients of Space, which of the following statement is correct?
  - A. At  $\alpha = 1\%$ , "Space" should be retained in the model.
  - B. At  $\alpha = 5\%$ , "Space" should not be retained in the model.
  - C. At  $\alpha = 10\%$ , "Space" should not be retained in the model.
  - D. At  $\alpha = 5\%$ , "Space" should not be retained in the model.
  - E. None of the above.
- 6. At 5% significant level, given Space = 70 and Water = 130 for a house, point estimate the electricity consumption.
  - A. In the range of [5000, 6000)
- B. In the range of [6000, 7000)
- C. In the range of [7000, 8000)
- D. In the range of [8000, 9000)
- E. In the range of [9000, 10000)
- 7. Determine whether the required conditions are satisfied.
  - A. The error variable's variance appears to be constant.
  - B. The histogram is slightly skewed and the errors are not normally distributed.
  - C. There is a strong correlation between the two independent variables.
  - D. Multicollinearity is a problem in this study.
  - E. None of the above.

Questions 8 through 13 are based on the following information.

The revenues (in millions of dollars) of a chain of ice cream stores are listed for each quarter during the years 1997-2001 as shown in the following table. Four-period centered moving average is given in column

4-p center MA. The ratio between y and 4-p center MA is also given in column v/MA

| Year | Quarter | # of Visitors (y) | 4-p center MA | v/MA    | Vear | Ouarter | # of Visitors (a) | y/1V1/A. |        |
|------|---------|-------------------|---------------|---------|------|---------|-------------------|----------|--------|
| 1997 | 1       | 16                | T             | 3/1/1/1 |      | Quarter |                   |          | y/MA   |
|      | 2       | 25                |               |         | 2000 | 1       | 18                | 29.125   | 0.6180 |
|      | 2       |                   |               |         |      | 2       | 29                | 29.375   | 0.9870 |
|      | 3       | 31                | 23.750        | 1.3050  |      | 3       | 45                | 29.375   | 1.5320 |
|      | 4       | 24                | 23.750        | 1.0110  |      | 4       | 24                | 29.875   | 0.8030 |
| 1998 | 1       | 14                | 24.125        | 0.5800  | 2001 | 1       | 21                |          |        |
|      | 2       | 27                | 24.125        | 1.1190  | -001 | 2       | 30                | 30.875   | 0.6800 |
|      | 3       | 32                | 24.375        | 1.3130  |      | 2       |                   | 32.750   | 0.9160 |
|      | 4       | 23                | 25.250        |         |      | 3       | 52                |          |        |
| 1999 | 1       |                   |               | 0.9110  |      | 4       | 32                |          |        |
| 1999 | 1       | 17                | 26.750        | 0.6360  |      |         |                   |          |        |
|      | 2       | 31                | 28.250        | 1.0970  |      |         |                   |          |        |
|      | 3       | 40                | 28.875        | 1.3850  |      |         |                   |          |        |
|      | 4       | 27                | 28.750        | 0.9390  |      |         |                   |          |        |

After the seasonal effect is removed, a regression model is built:  $\hat{y} = 20.2 + 0.732t$  where t starts from 1.

- 8. Which range does the seasonal index of the third quarter fall into?
  - A. In the range of [0.60, 0.90)
- B. In the range of [0,90, 1.20)
- C. In the range of [1.20, 1.50)
- D. In the range of [1.50, 1.80)
- E. In the range of [1.80, 2.10)
- 9. Use the seasonal indexes computed question 8 to deseasonalized the original time series data of the third quarter, 2000. Which range does it fall into?
  - A. In the range of [13, 19)
- B. In the range of [19, 23)
- C. In the range of [23, 28)
- D. In the range of [28, 32)

### 科目:統計學(B)

題號: 40

8 頁之第 4 頁

- E. In the range of [32, 36)
- 10. Which range does the seasonal index of the second quarter fall into?
  - A. In the range of [0.60, 0.90)
- B. In the range of [0.90, 1.20)
- C. In the range of [1.20, 1.50)
- D. In the range of [1.50, 1.80)
- E. In the range of [1.80, 2.10)
- 11. Use the seasonal indexes computed question 10 to deseasonalized the original time series data of the second quarter, 2001. Which range does it fall into?
  - A. In the range of [13, 19)
- B. In the range of [19, 23)
- C. In the range of [23, 28)
- D. In the range of [28, 32)
- E. In the range of [32, 36)
- 12. Use the seasonal indexes computed question 8 and the linear trend model given above to forecast the revenue in the third quarter, 2002. Which range does it fall into?
  - A. In the range of [27, 32)
- B. In the range of [32, 37)
- C. In the range of [37, 42)
- D. In the range of [42, 47)
- E. In the range of [47, 52)
- 13. Use the seasonal indexes computed question 10 and the linear trend model given above to forecast the revenue in the second quarter, 2002. Which range does it fall into?
  - A. In the range of [27, 32)
- B. In the range of [32, 37)
- C. In the range of [37, 42)
- D. In the range of [42, 47)
- E. In the range of [47, 52)

Questions 14 through 18 are based on the following information.

Pay equity for men and women has been an ongoing source of conflict for a number of years in North America. Suppose that a statistician is investigating the factors that affect salary differences between male and female university professors. The following variables are included in the study: Annual salary, number of years since first degree, highest degree (1 with a PhD and 0 else), Mean score on teaching evaluation, number of articles published, and gender (1 if male and 0 else). The result of the regression analysis is listed as follows.

| Regression Statistics |        |  |  |  |  |  |
|-----------------------|--------|--|--|--|--|--|
| Multiple R            | 0.9737 |  |  |  |  |  |
| R Square              | 0.9482 |  |  |  |  |  |
| Adjusted R Square     | 0.9454 |  |  |  |  |  |
| Standard Error        | 3015   |  |  |  |  |  |
| Observations          | 100    |  |  |  |  |  |

| Standard Lift |  |
|---------------|--|
| Observations  |  |
| ANOVA         |  |

| Sources    | df | SS          | MS         | F      | Significance F |
|------------|----|-------------|------------|--------|----------------|
| Regression | 5  | 15636303318 | 3127260664 | 344.04 | 0.0000         |
| Residual   | 94 | 854451113   | 9089905    |        | 0.0000         |
| Total      | 99 | 16490754431 |            |        |                |

|            | Coefficients | Standard Error | t Stat | P-value |
|------------|--------------|----------------|--------|---------|
| Intercept  | -5916        | 3141           | -1.88  | 0.0627  |
| Years      | 1022         | 48.93          | 20.88  | 0.0000  |
| PhD        | 725.7        | 961.5          | 0.75   | 0.4523  |
| Evaluation | 3729         | 619.8          | 6.02   | 0.0000  |
| Articles   | 439.1        | 80.69          | 5.44   | 0.0000  |
| Gender     | 1090         | 632.0          | 1.72   | 0.0879  |

- 14. In this problem, how many indicator variables are used?
  - A. 2

B. 3

C. 4

- D. 5
- E. None of the above.
- 15. Which of the following statement is correct?
  - A. Since F = 344.04, there is no evidence to infer that the model is valid.
  - B. Since p-value = 0, there is enough evidence to infer that the model is valid.

題號: 407

共 頁之第

- C. Since R Square = 0.9482, there is no evidence to infer that the model is valid.
- D. Since Standard Error = 3015, there is enough evidence to infer that the model is not valid.
- E. None of the above.
- 16. Which of the following statement is correct?
  - A. There is no evidence that the professors with PhD are better paid than the professors without PhD are at 10% significant level.
  - B. There is enough evidence that the professors with PhD are better paid than the professors without PhD are at 5% significant level.
  - C. There is no evidence that male professors are better paid than female professors are with the same qualifications at 10% significant level.
  - D. There is enough evidence that male professors are better paid than female professors are with the same qualifications at 5% significant level.
  - E. None of the above.
- 17. Point estimate the annual salary of a male professor with 20 years since first degree, PhD, 5 mean score on teaching evaluation, and 13 articles published.
  - A. In the range of [25000, 30000)
- B. In the range of [30000, 35000)
- C. In the range of [35000, 40000)
- D. In the range of [40000, 45000)
- E. In the range of [45000, 50000)
- 18. Point estimate the annual salary of a female professor with 20 years since first degree, PhD, 5 mean score on teaching evaluation, and 13 articles published.

  - A. In the range of [25000, 30000) B. In the range of [30000, 35000)
- C. In the range of [35000, 40000)

  D. In the range of [40000, 45000)

  E. In the range of [45000, 50000)
- 19. Suppose that the sample regression equation of a model is  $\hat{y} = 10 + 4x_1 + 3x_2 x_1x_2$ . If we examine the relationship between  $x_1$  and y for three different values of  $x_2$ , which of the following statement is correct?
  - A. Three equations produced differ only in the intercept
  - B. Three equations produced differ not only in the intercept term but the coefficient of  $x_1$ , also varies.
  - C. The coefficient of  $x_1$  varies.
  - D. The coefficient of  $x_2$  remains unchanged.
  - E. None of the above
- 20. Which of the following statements is correct in testing for normality?
  - A. The chi-squared test requires us to compute the mean and the standard deviation from the data.
  - B. The Kolmogorov-Smirnov test assumes that we can compute the mean and the standard deviation from the data.
  - C. The Lilliefors test requires relatively large samples to ensure its validity.
  - D. A Wilcoxon rank sum test can be used to test for normality but require very large samples.
  - E. None of the above

#### 三、簡答題(共 20 分):請按照題號順序作答

1. A major insurance firm interviewed a random sample of 1200 college students to find out the type of life insurance preferred, if any. The results follow:

#### Insurance Preference

| Gender | Term | Whole Life | No Insurance |
|--------|------|------------|--------------|
| Female | 100  | 80         | 325          |
| Male   | 160  | 60         | 475          |

The firm tries to answer the question of "is there evidence that life insurance preference of male students is different than that of female students?"

- (1) (1 分)Please write down the testing hypotheses.
- (2) (4分)Please choose the testing method, compute the test statistics, and make conclusion.

科目:統計學(B)

題號:4

共 8 頁之第 6 頁

2. A professor of statistics is trying to determine which of three statistical software's is the best for his students. He believes that the time (in hours) it takes a student to master a particular software may be influenced by gender. The ANOVA analysis result is as follows. (Please write down hypotheses, testing procedure, and conclusion in the following tests.)

|                     | 6       |    |         |        |         |            |
|---------------------|---------|----|---------|--------|---------|------------|
| SOURCE OF VARIATION | SS      | DF | MS      | F      | P-VALUE | F-CRITICAL |
| Software            | 25.333  | 2  | 12.667  | 1.194  | .3367   | 3.885      |
| Gender              | 107.556 | 1  | 107.556 | 10.136 | .0079   | 4.747      |
| Interaction         | 61.778  | 2  | 30.889  | 2.911  | .0932   | 3.885      |
| Errors              | 127.333 | 12 | 10.611  |        |         |            |
| Total               | 322.000 | 17 |         |        |         |            |

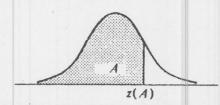
- (1) (3 分)Is there sufficient evidence at the 5% significance level to infer that different software results in different time for a student to master?
- (2) (3 分)Is there sufficient evidence at the 5% significance level to infer that different gender causes different time for a student to master a software?
- (3) (3 分)Is there sufficient evidence at the 5% significance level to infer that the time it takes a student to master a software and the gender of the student interact?
- 3. (1) (2 分)What is the nonparametric method to compare two populations, when the samples are matched pairs and the data are quantitative where the normality requirement necessary to perform the parametric test is unsatisfied?
  - (2) (2分)What is the nonparametric method to compare two populations, when the samples are matched pairs and the data are ranked?
  - (3) (2 分)What is the nonparametric method to compare two or more populations, when the samples are matched pairs and the data are either ranked or quantitative but not normal?

題號:407

共8頁之第7頁

# Cumulative Probabilities of the Standard Normal Distribution

Entry is area A under the standard normal curve from  $-\infty$  to z(A)



| -   |           |            |       | LE MANAGEMENT - LE LA COMPANION - LE LA COMPANIO |          |       |       |       |   |       |
|-----|-----------|------------|-------|--|----------|-------|-------|-------|---|-------|
| z   | .00       | .01        | .02   | .03  | .04      | .05   | .06   | .07   | .08   | .09   |
| .0  | .5000     | .5040      | .5080 | .5120  | .5160    | .5199 | .5239 | .5279 | .5319   | .5359 |
| .1  | .5398     | .5438      | .5478 | .5517  | .5557    | .5596 | .5636 | .5675 | .5714   | .5753 |
| .2  | .5793     | .5832      | .5871 | .5910  | .5948    | .5987 | .6026 | .6064 | .6103   | .6141 |
| .3  | .6179     | .6217      | .6255 | .6293  | .6331    | .6368 | .6406 | .6443 | .6480   | .6517 |
| .4  | .6554     | .6591      | .6628 | .6664  | .6700    | .6736 | .6772 | .6808 | .6844   | .6879 |
| .5  | .6915     | .6950      | .6985 | .7019  | .7054    | .7088 | .7123 | .7157 | .7190   | .7224 |
| .6  | .7257     | .7291      | .7324 | .7357  | 7389     | .7422 | .7454 | .7486 | .7517   | .7549 |
| .7  | .7580     | .7611      | .7642 | .7673  | .7704    | .7734 | .7764 | .7794 | .7823   | .7852 |
| .8  | .7881     | .7910      | .7939 | 7967   | 7995     | .8023 | .8051 | .8078 | .8106   | .8133 |
| .9  | .8159     | .8186      | .8212 | .8238  | .8264    | .8289 | .8315 | .8340 | .8365   | .8389 |
| 1.0 | .8413     | .8438      | .8461 | 1.8485   | 8508     | .8531 | .8554 | .8577 | .8599   | .8621 |
| 1.1 | .8643     | .8665      | .8686 | 8708   | 0.8729   | .8749 | .8770 | .8790 | .8810   | .8830 |
| 1.2 | .8849     | .8869      | .8888 | .8907  | .8925    | .8944 | .8962 | .8980 | .8997   | .9015 |
| 1.3 | .9032     | .9049      | .9066 | .9082  | .9099    | .9115 | 9131  | .9147 | .9162   | .9177 |
| 1.4 | .9192     | .9207      | .9222 | .9236  | .9251    | .9265 | .9279 | .9292 | .9306   | .9319 |
| 1.5 | .9332     | .9345      | .9357 | .9370  | .9382    | 9394  | .9406 | .9418 | .9429   | .9441 |
| 1.6 | .9452     | .9463      | .9474 |  | 9495     |       | .9515 | .9525 | .9535   | .9545 |
| 1.7 | .9554     | .9564      | .9573 | .9582  | .9591    | .9599 | .9608 | .9616 | .9625   | .9633 |
| 1.8 | .9641     | .9649      | .9656 | .9664  | .9671    | .9678 | .9686 | .9693 | .9699   | .9706 |
| 1.9 | .9713     | .9719      | .9726 | .9732  | .9738    | .9744 | .9750 | .9756 | .9761   | .9767 |
| 2.0 | .9772     | .9778      | .9783 | .9788  | .9793    | .9798 | .9803 | .9808 | .9812   | .9817 |
| 2.1 | .9821     | .9826      | .9830 | .9834  | .9838    | .9842 | .9846 | .9850 | .9854   | .9857 |
| 2.2 | .9861     | .9864      | .9868 | .9871  | .9875    | .9878 | .9881 | .9884 | .9887   | .9890 |
| 2.3 | .9893     | .9896      | .9898 | .9901  | .9904    | .9906 | .9909 | .9911 | .9913   | .9916 |
| 2.4 | .9918     | .9920      | .9922 | .9925  | .9927    | .9929 | .9931 | .9932 | .9934   | .9936 |
| 2.5 | .9938     | .9940      | .9941 | .9943  | .9945    | .9946 | .9948 | .9949 | .9951   | .9952 |
| 2.6 | .9953     | .9955      | .9956 | .9957  | .9959    | .9960 | .9961 | .9962 | .9963   | .9964 |
| 2.7 | .9965     | .9966      | .9967 | .9968  | .9969    | .9970 | .9971 | .9972 | .9973   | .9974 |
| 2.8 | .9974     | .9975      | .9976 | .9977  | .9977    | .9978 | .9979 | .9979 | .9980   | .9981 |
| 2.9 | .9981     | .9982      | .9982 | .9983  | .9984    | .9984 | .9985 | .9985 | .9986   | .9986 |
| 3.0 | .9987     | .9987      | .9987 | .9988  | .9988    | .9989 | .9989 | .9989 | .9990   | .9990 |
| 3.1 | .9990     | .9991      | .9991 | .9991  | .9992    | .9992 | .9992 | .9992 | .9993   | .9993 |
| 3.2 | .9993     | .9993      | .9994 | .9994  | .9994    | .9994 | .9994 | .9995 | .9995   | .9995 |
| 3.3 | .9995     | .9995      | .9995 | .9996  | .9996    | .9996 | .9996 | .9996 | .9996   | .9997 |
| 3.4 | .9997     | .9997      | .9997 | .9997  | .9997    | .9997 | .9997 | .9997 | .9997   | .9998 |
|     |           |            |       | ~ 4  |          |       |       | y     | gyfrediging hydrodyn, awy grawyr felliwerth abard |       |
| C   |           |            |       |  | ted Perc |       | 00 1  |       | 000   | 1     |
| Cum | ulative p | robability | / A:  | .90  | .95      | .975  | .98   | .99   | .995  | .999  |
|     |           | 21         | (A):  | 1.282  | 1.645    | 1.960 | 2.054 | 2.326 | 2.576   | 3.090 |
|     |           |            |       |  |          |       |       |       |   |       |

# 接背面

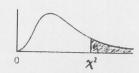
科目:統計學(B)

題號:407

共8頁之第8頁

## CHI-SQUARE DISTRIBUTION TABLE

The entries in the table give the critical values of  $\chi^2$  for the specified number of degrees of freedom and areas in the right tail.



|     |        |        | Area   | in the Righ | t Tail under | the Chi-sar | are Distribu | tion Curve |         |         |
|-----|--------|--------|--------|-------------|--------------|-------------|--------------|------------|---------|---------|
| df  | .995   | .990   | .975   | .950        | .900         | .100        | .050         | .025       | .010    | .005    |
| 1   | 0.000  | 0.000  | 0.001  | 0.004       | 0.016        | 2.706       | 3.841        | 5.024      | 6.635   | 7.879   |
| 2   | 0.010  | 0.020  | 0.051  | 0.103       | 0.211        | 4.605       | 5.991        | 7.378      | 9.210   | 10.597  |
| 3   | 0.072  | 0.115  | 0.216  | 0.352       | 0.584        | 6.251       | 7.815        | 9.348      | 11.345  | 12.838  |
| 4   | 0.207  | 0.297  | 0.484  | 0.711       | 1.064        | 7.779       | 9.488        | 11.143     | 13.277  | 14.860  |
| 5   | 0.412  | 0.554  | 0.831  | 1.145       | 1.610        | 9.236       | 11.070       | 12.833     | 15.086  | 16.750  |
| 6   | 0.676  | 0.872  | 1.237  | 1.635       | 2.204        | 10.645      | 12.592       | 14.449     | 16.812  | 18.548  |
| 7   | 0.989  | 1.239  | 1.690  | 2.167       | 2.833        | 12.017      | 14.067       | 16.013     | 18.475  | 20.278  |
| 8   | 1.344  | 1.646  | 2.180  | 2.733       | 3.490        |             | 15.507       | 17.535     | 20.090  | 21.955  |
| 9   | 1.735  | 2.088  | 2.700  | 3.325       | 4.168        | 14.684      | 16.919       | 19.023     | 21.666  | 23.589  |
| 11) | 2.156  | 2.558  | 3.247  | 3.940       | 4.865        | 15.987      | 18.307       | 20.483     | 23.209  | 25.188  |
| 11  | 2.603  | 3.053  | 3.816  | 4.575       | 5.578        | 17.275      | 19.675       | 21.920     | 24.725  | 26.757  |
| 12  | 3.074  | 3.571  | 4.404  | 5.226       |              | 18.549      | 21.026       | 23.337     | 26.217  | 28.300  |
| 13. | 3.565  | 4.107  | 5.009  | 5.892       | 7.042        | 19.812      | 22.362       | 24.736     | 27.688  | 29.819  |
| 14  | 4.075  | 4.660  | 5.629  | 6.571       | 7.790        | 21.064      | - 23.685     | 26.119     | 29.141  | 31.319  |
| 15  | 4.601  | 5.229  | 6.262  | 7.261       | 8.547        | 22,307      | 24.996       | 27.488     | 30.578  | 32.801  |
| 16  | 5.142  | 5.812  | 6.908  | 7.962       | 9.312        | 23.542      | 26.296       | 28.845     | 32.000  | 34.267  |
| 17  | 5.697  | 6.408  | 7.564  | 8.672       | 10.085       | 24.769      |              | 30.191     | 33.409  | 35.718  |
| 18  | 6.265  | 7.015  | 8.231  | 9.390       | 10.865       | 25.989      | 28.869       | 31.526     | 34.805  | 37.156  |
| 19  | 6.844  | 7.633  | 8.907  | 10.117      | 17.651       | 27.204      | 30.144       | 32.852     | 36.191  | 38.582  |
| 20  | 7.434  | 8.260  | 9.591  | 10.851      | 12.443       | 28.412      | 31.410       | 34.170     | 37.566  | 39.997  |
| 21  | 8.034  | 8.897  | 10.283 | 11.591      | 13.240       | 29.615      | 32.671       | 35.479     | 38.932  | 41.401  |
| 22  | 8.643  | 9.542  | 10.982 | 12.338      | 14.041       | 30.813      | 33.924       | 36.781     | 40.289  | 42.796  |
| 23  | 9.260  | 10.196 | 11.689 | 13.091      | 14.848       | 32.007      | 35.172       | 38.076     | 41.638  | 44.181  |
| 24  | 9.886  | 10.856 | 12.401 | 13.848      | 15.659       | 33.196      | 36.415       | 39.364     | 42.980  | 45.559  |
| 25  | 10.520 | 11.524 | 13.120 | 14.611      | 16.473       | 34.382      | 37.652       | 40.646     | 44.314  | 46.928  |
| 26  | 11.160 | 12.198 | 13.844 | 15.379      | 17.292       | 35.563      | 38.885       | 41.923     | 45.642  | 48.290  |
| 27  | 11.808 | 12.879 | 14.573 | 16.151      | 18.114       | 36.741      | 40.113       | 43.195     | 46.963  | 49.645  |
| 28  | 12.461 | 13.565 | 15.308 | 16.928      | 18.939       | 37.916      | 41.337       | 44.461     | 48.278  | 50.993  |
| 29  | 13.121 | 14.256 | 16.047 | 17.708      | 19.768       | 39.087      | 42.557       | 45.722     | 49.588  | 52.336  |
| 30  | 13.787 | 14.953 | 16.791 | 18.493      | 20.599       | 40.256      | 43.773       | 46.979     | 50.892  | 53.672  |
| 40  | 20.707 | 22.164 | 24.433 | 26.509      | 29.051       | 51.805      | 55.758       | 59.342     | 63.691  | 66.766  |
| 50  | 27.991 | 29.707 | 32.357 | 34.764      | 37.689       | 63.167      | 67.505       | 71.420     | 76.154  | 79.490  |
| 60  | 35.534 | 37.485 | 40.482 | 43.188      | 46.459       | 74.397      | 79.082       | 83.298     | 88.379  | 91.952  |
| 70  | 43.275 | 45.442 | 48.758 | 51.739      | 55.329       | 85.527      | 90.531       | 95.023     | 100.425 | 104.215 |
| 80  | 51.172 | 53.540 | 57.153 | 60.391      | 64.278       | 96.578      | 101.879      | 106.629    | 112.329 | 116.321 |
| 90  | 59.196 | 61.754 | 65.647 | 69.126      | 73.291       | 107.565     | 113.145      | 118.136    | 124.116 | 128.299 |
| 100 | 67.328 | 70.065 | 74.222 | 77.929      | 82.358       | 118.498     | 124.342      | 129.561    | 135.807 | 140.169 |