

1. (5% each; 20% in total) Consider the asymptotic growth rates of the following.

- (a). $(\lg n)!$ (b). $\lg(n!)$ (c). $4^{\lg n}$ (d). $(\frac{3}{2})^n$

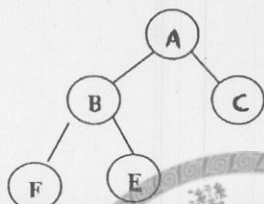
Answer the following questions by T (true) or F (false)

- (1) the order of (a) is greater than the order of (c)
- (2) the order of (a) is greater than the order of (d)
- (3) the order of (b) is greater than the order of (c)
- (4) the order of (b) is greater than the order of (d)

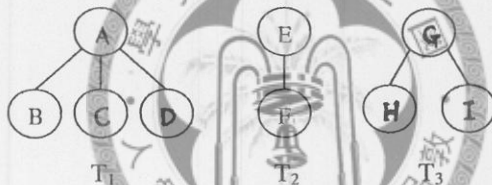
2. (a) (10%) Write the postfix form of the following expression:

$$D/(A+B)+C)*D-C*D$$

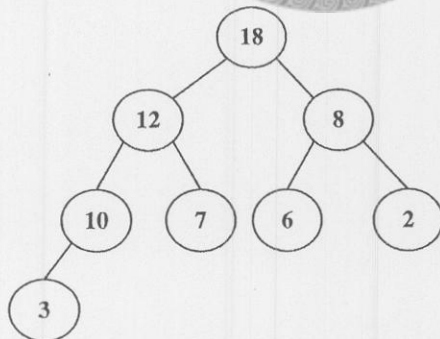
(b) (10%) What are the sequences of the post order traversals of the following tree?



3. (a) (10%) Draw the binary tree representation of $B(T_2, T_1, T_3)$.



(b) (10%) Draw the resulting max heap if node with value 18 in the following is deleted.



4. (a) (10%) Please draw the binary tree with the following information

Inorder Traversal: CBEDFAIHKJGLM

Preorder Traversal: ABCDEFGHIJKLM

(b) (10%) How many different ways can we perform the multiplications when we compute the product of 15 matrices: $M_1 \times M_2 \times \dots \times M_{15}$.

5. (a) (10%) Please construct an AVL tree by adding the following item in order: MARCH, MAY, AUGUST, OCTOBER, AUGUST, APRIL, JUNE, FEBRAURY, DECEMBER, JANUARY, JULY, SEPTEMBER. (Please show the balance factor of each node in each step. Note that the comparison is based on alpha-beta order, e.g., MAY > AUGUST and MARCH > JANUARY.)

(b) (10%) If a tree with only one node is defined as height 1. What is the maximum and minimum height of an AVL tree with 400 nodes?