- 1. Find the number of different binary trees with 5 nodes. (16 points)
- 2. Given the matrix

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}$$

Draw a graph that has A as its adjacency matrix. Be sure to label the vertices of the graph. (16 points)

- 3. Demonstrate the insertion of the keys 15, 18, 29, 13, 21, 35, 11, 12, 10 into a hash table with collisions resolved by chaining. Let the table have 9 slots (0..8), and let the hash function be h(k)=k mod 9. (18 points)
- 4. Suppose that  $\sum_{k=1}^{n} k^5 = \Theta(n^a)$ ,  $\sum_{k=1}^{n} (\log k)^2 = \Theta(n^b (\log n)^c)$ , and  $\sum_{k=1}^{n} k^2 (\log k)^3 = \Theta(n^a (\log n)^c)$ . Find the value of the constants a, b, c, d, e. (15 points)
- 5. Given a set { 6.0, 1.1, 2.3, 3.4, 2.5, 1.2, 2.0, 3.3, 5.2, 3.6, 4.7, 4.5} of points on the real line. Find a smallest set of unit-length closed intervals that contains all of the given points. (15 points)
- 6. Describe how to use depth first search to determine whether the input directed graph G = (V, E) is acyclic.
  (20 points)