

Fig. 1

Problem 1. A L-shaped structure retains water at the top of a dam. The width of the structure (normal to the piece of paper) is W . A force F is needed to keep the structure from tumbling down. Assume that dimensions W, H, L, B and D are known.

- Find F when only water at rest is present (see panel a of the figure);
- Find F when a sphere floats on the water surface and a cube rests on the bottom flange of the L-shaped structure (as shown on panel b of the figure).
- Find F when water flows out through a Borda orifice of diameter D (as shown on panel c).

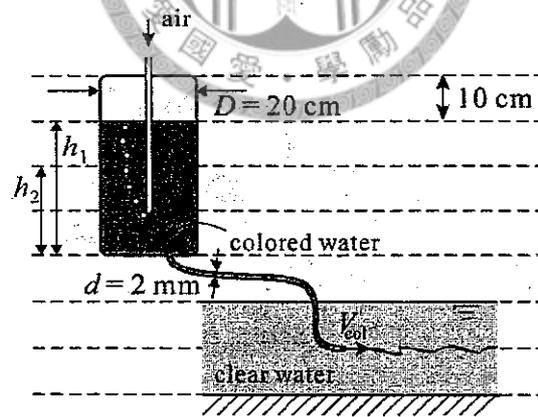


Fig. 2

Problem 2. To visualize water motions, colored water is introduced in a channel of clear water using a Mariotte bottle (see figure) of diameter D . The colored water inside the bottle is in contact with the atmosphere through a thin tube which lets air enter. Assume inviscid flow.

- Find the velocity V_{col} of the colored water at the outlet of the pipe (of diameter d), when the level of colored water in the bottle is equal to h_1 .
- Find V_{col} when the level of colored water in the bottle is equal to h_2 .
- Find the time t needed for the colored water level to drop from h_1 to h_2 .

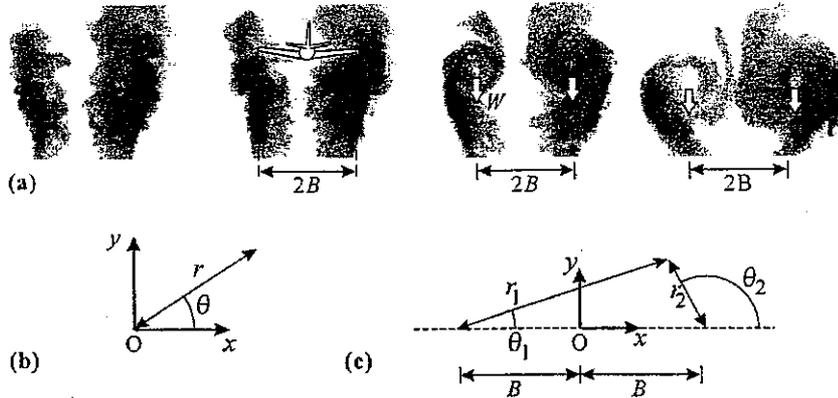


Fig. 3

Problem 3. Due to the passage of an airplane, two vortices of equal strength rotating in opposite directions are created, and move down at constant velocity W . A steady flow is seen by an observer moving with the two vortices.

- Using the coordinates of Fig. 3c, formulate the potential ϕ of this steady flow.
- Check that your potential satisfies the Laplace equation $\nabla^2\phi = 0$.
- Find the streamfunction ψ of this steady flow.
- Draw the streamlines of this steady flow.
- Find the maximum air pressure p_{\max} and indicate where this pressure occurs.

Hint: the potential for a single vortex is given in polar coordinates by $\phi(r, \theta) = \frac{\Gamma}{2\pi} \theta$.

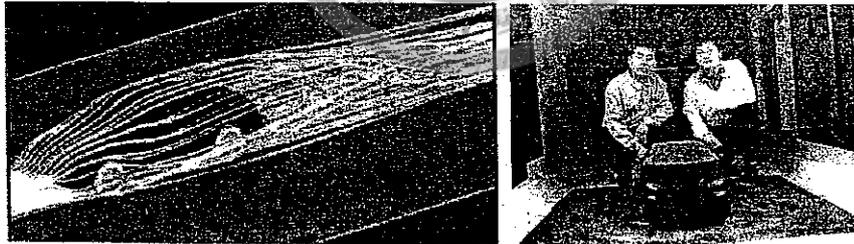


Fig. 4

Problem 4. The drag force F_D exerted by air on a car moving at speed V is given by

$$F_D = F(B, H, V, \rho, \mu)$$

where B = width and H = height of the car. Wind tunnel tests using air at atmospheric pressure are conducted with a car model of scale 1:3 (three times smaller than reality).

- Find a non-dimensional relationship for F_D .
- Find the model air speed V_m corresponding to the real car speed $V = 100$ km/h.
- At the speed V_m found in b), the measured drag force for the car model is $F_{Dm} = 300$ N. Find the predicted drag force F_D for the real car at speed $V = 100$ km/h.

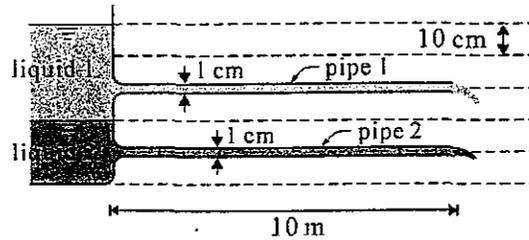


Fig. 5

Problem 5. Two liquids flow out of the same tank through two pipes as shown on the Figure above. Liquid 1 has density $\rho_1 = 1000 \text{ kg/m}^3$ and kinematic viscosity $\nu_1 = 1 \times 10^{-6} \text{ m}^2/\text{s}$. Liquid 2 has density $\rho_2 = 2000 \text{ kg/m}^3$ and kinematic viscosity $\nu_2 = 1 \times 10^{-3} \text{ m}^2/\text{s}$. Assume that the flow is laminar and that the friction coefficient is

$$f = \frac{64\mu}{\rho V D}$$

- Find Q_1 = discharge of liquid 1 through pipe 1.
- Find Q_2 = discharge of liquid 2 through pipe 2.
- Calculate the Reynolds numbers Re_1 and Re_2 in each pipe.
- Was it correct to assume laminar flow in pipe 1 and in pipe 2?
- Derive the formula above for the laminar friction coefficient f .

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