

※注意：選擇題部分請於試卷之「選擇題作答區」內作答

- 1 至 15 為單選選擇題(每題 5 分, 答錯不倒扣。 Also, “ $x \bmod y$ ” means “the remainder after  $x$  is divided by  $y$ ”. For example,  $8 \bmod 5=3$ ,  $27 \bmod 5=2$ , and  $20 \bmod 5=0$ .)

**Questions 1 and 2:** The following items are ordered by their asymptotic growth rates as  $X_1 < X_2 < X_3 < X_4 < X_5$ ,

(i)  $(n-1)!$  (ii)  $4^{\lg n}$  (iii)  $(\lg n)^{\lg n}$  (iv)  $(\frac{4}{3})^n$  (v)  $\lg(n!)$

1. What is  $X_2$ ?

(A)  $(n-1)!$  (B)  $4^{\lg n}$  (C)  $(\lg n)^{\lg n}$  (D)  $(\frac{4}{3})^n$  (E)  $\lg(n!)$

2. What is  $X_4$ ?

(A)  $(n-1)!$  (B)  $4^{\lg n}$  (C)  $(\lg n)^{\lg n}$  (D)  $(\frac{4}{3})^n$  (E)  $\lg(n!)$

**Questions 3 and 4:** Let  $A=1$ ,  $B=2$ ,  $C=3$ ,  $D=4$ , and  $E=5$ .

3. Let the value of the postfix expression:

$AB + D \times EBA // + AD \times C / + CD \times + A - B + CD \times -$

be  $y$ . Then,  $y \bmod 5 = ?$

(A) 0 (B) 1 (C) 2 (D) 3 (E) 4

4. Let the value of the prefix expression:  $+ \times + ABC \times + \times D \times E + DE \times ABC$

be  $z$ . Then,  $z \bmod 5 = ?$

(A) 0 (B) 1 (C) 2 (D) 3 (E) 4

**Questions 5 and 6:** Let  $X_1, X_2, \dots, X_{13}$  be the postorder traversal of a binary tree which has the following information.

Its inorder traversal: CAEDFBGCHKJILM

Its preorder traversal: BACDEFIHGJKLM

Then,

5.  $X_3 =$

(A) C (B) F (C) D (D) I (E) 以上皆非

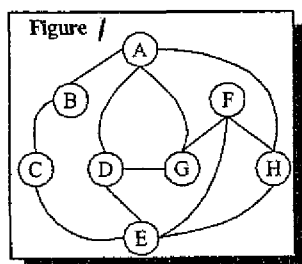
6.  $X_6 =$

(A) C (B) F (C) D (D) I (E) 以上皆非

7. Let  $X_1, X_2, \dots, X_8$  be the order of nodes visited by applying BFS in Fig 1, starting from node A (visited in the lexical order),  $X_6 = ?$

(A) A (B) C (C) D (D) G (E) 以上皆非

8. Let  $X_1, X_2, \dots, X_8$  be the order of nodes visited by applying DFS in Fig 1, starting from node A (visited in the lexical order),  $X_6 = ?$



(A) A (B) C (C) D (D) G  
(E) 以上皆非

Questions 9 and 10: Suppose an AOE network is shown in Figure 2

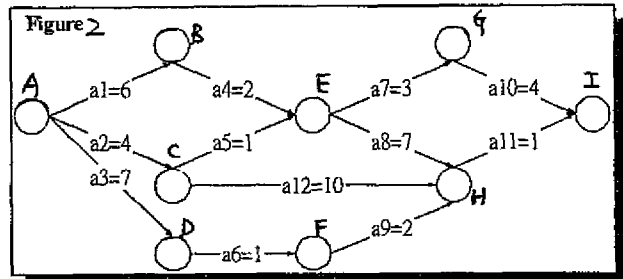
9. Let  $e(i)$  denote the earliest time of activity  $a_i$ .

What is  $(e(11) \bmod 5)$ ?

- (A) 0 (B) 1 (C) 2 (D) 3  
(E) 4

10. Let  $l(i)$  denote the latest time of activity  $a_i$ . What is  $(l(9) \bmod 5)$ ?

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4



11. Suppose a tree with only one node is defined to be with height 1. Let  $x$  be the maximum height of an AVL tree with 400 nodes. Then,  $x \bmod 5 = ?$

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

12. Suppose a tree with only one node is defined to be with height 1. Let  $y$  be the minimum height of an AVL tree with 400 nodes. Then,  $y \bmod 5 = ?$

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

13. Let  $b$  be the number of different ways we can perform the multiplications for the product of 6 matrices:  $M_1 \times M_2 \times \dots \times M_6$ . Then  $b \bmod 5 = ?$

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

Questions 14 and 15: Let  $T_B$  be the binary tree representation of  $B(T_1, T_2, T_3)$

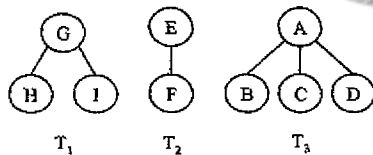


Figure 3

14. Let  $X_1, X_2, \dots, X_9$  be the inorder traversal on this tree  $T_B$ .  $X_6 = ?$

- (A) H (B) I (C) B (D) A (E) 以上皆非

15. Let  $Y_1, Y_2, \dots, Y_9$  be the postorder traversal on this tree  $T_B$ .  $Y_6 = ?$

- (A) H (B) I (C) B (D) A (E) 以上皆非

16. (共 25 分) By inserting the following items in order: 25, 14, 30, 18, 35, 7, 5, and 27, please construct and draw, respectively, (a) a deap (5%) (b) a min-max heap (10%) (c) AVL tree (10%)