國立台灣大學九十四學年度碩士班招生考試試題

科目:應用數學(A)

題號:457

共/頁之第全頁

1.(10%) Find
$$\int_{\theta}^{\infty} e^{-ax} \cos(bx) dx$$
, with $a > \theta$.

2.(10%) Find
$$\int_{\theta}^{\frac{\pi}{2}} \frac{\sin\theta \cos\theta}{1 + \sin^4\theta} d\theta$$

3.(20%) Solve $\frac{dy}{dx} = xe^{x-y}$ with the boundary condition: $y = \ln 2$ at x = 0.

4.(10%) Triangularize the matrix:
$$\begin{bmatrix} -2 & 1 & 0 & 3 \\ 1 & -3 & 2 & 4 \\ 3 & 0 & 2 & -1 \\ 2 & -2 & 4 & 6 \end{bmatrix}$$

5.(10%) Find the eigenvalues and determine the rank of the matrix: $\begin{bmatrix} 1 & 1 \\ a & a^2 \end{bmatrix}$.

6.(20%) Find the Fourier series expansion of the periodic function: f(x) = |x| for $-\pi < x \le \pi$, and period = 2π .

- 7.(10%) If we pick 10 telephone numbers at random from a telephone book and record the last digit of the numbers, what is the probability that we obtain each of the integers from 0 to 9 once only?