

1. Please give the definitions of Reynolds number and vorticity. (20%)

2. A velocity field is

$$V = (x^2 + y^2 + x)i - (2xy + y)j.$$

Does this velocity field represent a possible irrotational flow? (20%)

3. Please write down the Navier-Stokes Equation in Cartesian Coordinates

(x, y, z) and explain the physical mean of each term. (20%)

4. The velocity potential of steady flow is given as

$$\phi = x^2 + y^3 - 5z$$

The temperature field is given as

$$T = x + 3xy^2 + z^2 + 5xyz$$

Estimate the time rate of change of temperature of a fluid element as it passes through the point $(2, 0, -3)$. (20%)

5. What is the stream function? If the stream function can be expressed as

$$\psi = -Ay + Be^{-y} \cos x$$

Please write down its velocity field and vorticity. (20%)