

## I. 單選題 (每題5分) ※注意：請於試卷「選擇題作答區」依題號作答。

A staff member for a political campaign estimated the model  $V_t = \alpha + \beta P_t + \mu_t$ , for  $t = 1, 2, \dots, 22$ . where  $V_t$  is voter turnout in precinct  $t$ , and  $P_t$  is the precinct's population. When the results were being printed out, the printer malfunctioned, smudging some of the results. With the information already provided, answer questions 1-6.

Coefficient	Estimate	Standard Error	t-ratio
$\hat{\alpha}$	26.034	—	14.955
$\hat{\beta}$	0.137	0.028	—
ESS=305.96	$\bar{P} = 54.478$	$s_V^2 = 31.954$	$s_P^2 = 925.91$
$r_{VP} = \underline{\hspace{2cm}}$	$R^2 = \underline{\hspace{2cm}}$	$\hat{\sigma}^2 = \underline{\hspace{2cm}}$	$\bar{V} = \underline{\hspace{2cm}}$

Note: ESS is Error Sum of Squares.

$r_{VP}$  is the simple correlation between  $V$  and  $P$ .

1. The standard error of  $\hat{\alpha}$  is  
 (A) 1.7408    (B) 1.5231    (C) 2.7233    (D) 0.2441
2. The t-ratio of  $\hat{\beta}$  is  
 (A) 5.244    (B) 4.893    (C) 2.144    (D) 0.204
3. The value of  $\hat{\sigma}^2 = \underline{\hspace{2cm}}$   
 (A) 14.570    (B) 13.907    (C) 15.298    (D) 46.295
4. The value of  $R^2 = \underline{\hspace{2cm}}$   
 (A) 0.456    (B) 0.016    (C) 0.544    (D) 0.189
5. The value of  $r_{VP} = \underline{\hspace{2cm}}$   
 (A) 0.675    (B) 0.125    (C) 0.437    (D) 0.738
6. The value of  $\bar{V} = \underline{\hspace{2cm}}$   
 (A) 7.463    (B) 5.616    (C) 702.988    (D) 33.497

7. Which of the following is not a test for serial correlation?

(A) The Durbin-Watson test.                   (B) The Bartlett test.  
(C) The Breusch-Godfrey LM test.             (D) The portmanteau  $Q$  test.

8. Mean absolute percentage error (MAPE) (平均絕對百分比誤差) is defined as

$\frac{1}{K} \sum_{t=N+1}^{N+K} \left| \frac{\hat{F}_t - F_t}{F_t} \right| \times 100$ , where  $\hat{F}_t$  and  $F_t$  represent the forecast and actual

values, and  $K$  is the number of forecast observations in the estimation period. The summation runs from  $t = N + 1$  to  $N + K$ . Which of the following statements about MAPE is correct?

- (A) MAPE is not very useful, because positive errors are canceled by negative errors, and the mean is always close to zero.
  - (B) We use MAPE when the magnitude of the error is more important than the direction of the error.
  - (C) MAPE penalizes large errors more sever than the root mean square error (均方根誤差) measure.
  - (D) MAPE is usually a better performance criterion if the actual values are close to zero.

9. A regression model is specified as  $Y_i = \alpha + \beta X_i + \varepsilon_i$ . If  $\hat{\alpha}$  and  $\hat{\beta}$  are the least square estimators of  $\alpha$  and  $\beta$  and the sample mean  $\bar{X}$  is zero, then

- (A)  $\text{cov}(\hat{\alpha}, \hat{\beta}) < 0$       (B)  $\text{cov}(\hat{\alpha}, \hat{\beta}) = \infty$   
 (C)  $\text{cov}(\hat{\alpha}, \hat{\beta})$  is indeterminate      (D)  $\text{cov}(\hat{\alpha}, \hat{\beta}) = 0$

10. Which of the following statements is incorrect?

- (A) When the disturbances are heteroskedastic but their “average” variance in the first part of the sample is not too different from that in the second part, the Goldfield-Quandt test has a high probability of accepting  $H_0$  when it is false.
  - (B) The Breusch-Pagan test has been criticized on the grounds that it is very sensitive to minor violations of the assumption of normality of the regression disturbance.
  - (C) Durbin developed two asymptotic (and asymptotically equivalent) tests, the  $h$  test and the  $m$  test for regression model when the explanatory variable—or one of the explanatory variables—is a lagged dependent variable.
  - (D) The Durbin-Watson test is not reasonably robust with respect to non-normality or heteroskedasticity of the disturbances.

- II** 1. The primary determinant of the amount of vacation time U.S. employees receive is their length of service. According to data released by Hewitt Associates (*Management Review*, Nov. 1995), more than 8 of 10 employers provide 2 weeks of vacation after the first year. After 5 years, 75 % of employers provide 3 weeks and after 15 years most provide to 4-week vacations. To more accurately estimate  $p$ , the proportion of U.S. employers who provide only 2 weeks of vacation to new hires, a random sample of 24 major U.S. companies was contacted. The following vacation times were reported (in days):

VACTIMES

10	12	10	10	10	10
15	10	10	10	10	10
10	10	10	10	10	15
10	10	15	10	10	10

- a. Construct a 95 % confidence interval for  $p$ . (10 分)
- b. Is the sample size large enough to ensure that the normal distribution provides a reasonable approximation to the sampling distribution of  $\hat{p}$ ? Justify your answer. (10 分)
- c. How large a sample would be required to estimate  $p$  to within .02 with 95 % confidence? (5 分)
2. Each year, approximately 1.3million Americans suffer adverse drug effects (ADEs)—that is ,unintended injuries caused by prescribed medication . A study in the *Journal of the American Medical Association* (July 5, 1995) identified the cause of 247 ADEs that occurred at two Boston hospitals. The researchers found that dosing errors (that is, wrong dosage prescribed and/or dispensed) were the most common. The next table summarizes the proximate cause of 95 ADEs that resulted from a dosing error. Conduct a test (at  $\alpha = .10$ ) to determine whether the true percentages of ADEs in the five “cause” categories are different. (10 分)

ADE

Wrong Dosage Cause	Number of ADEs
(1) Lack of knowledge of drug	29
(2) Rule violation	17
(3) Faulty dose checking	13
(4) Slips	9
(5) Other	27

3. Suppose the Total Sum of Squares for a completely randomized design with  $k = 6$  treatments and  $n = 36$  total measurements (six per treatment) is equal to 500. In each of the following cases, conduct an  $F$ -test of the null hypothesis that the mean responses for the five treatments are the same. Use  $\alpha = .10$ .
- Sum of Squares for Treatments (SST) is 20 % of SS (Total) (5 分)
  - SST is 80 % of SS (Total) (5 分)
  - What happens to the  $F$ -ratio as the percentage of the Total Sum of Squares attributable to treatments is increased? (5 分)

**TABLE A.1** Areas under the Standard Normal Curve from 0 to  $z$ 

$z$	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2518	0.2549
0.7	0.2580	0.2612	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.49865	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
4.0	0.49997									

Note: If  $z = 0.98$ ,  $p(0 \leq Z \leq z) = 0.3238$ .

Source: *Statistical Analysis for Decision Making*, Morris Hamburg, 4th edition, 1987. Reprinted with the permission of Harcourt Brace College Publishers.

TABLE A.2 Percentage Points of the t-Distribution

d.f.	1T = 0.4	0.25	0.1	0.05	0.025	0.01	0.005	0.0025	0.001	0.0005
	2T = 0.8	0.5	0.2	0.1	0.05	0.02	0.01	0.005	0.002	0.001
1	0.325	1.000	3.078	6.314	12.706	31.821	63.657	127.32	318.31	636.62
2	.289	0.816	1.886	2.920	4.303	6.965	9.925	14.089	22.327	31.598
3	.277	.765	1.638	2.353	3.182	4.541	5.841	7.453	10.214	12.924
4	.271	.741	1.538	2.132	2.776	3.747	4.604	5.598	7.173	8.610
5	0.267	0.727	1.476	2.015	2.571	3.365	4.032	4.773	5.893	6.869
6	.265	.718	1.440	1.943	2.447	3.143	3.707	4.317	5.208	5.959
7	.263	.711	1.415	1.895	2.365	2.998	3.499	4.029	4.785	5.408
8	.262	.706	1.397	1.860	2.306	2.896	3.355	3.833	4.501	5.041
9	.261	.703	1.383	1.833	2.262	2.821	3.250	3.690	4.297	4.781
10	0.260	0.700	1.372	1.812	2.228	2.764	3.169	3.581	4.144	4.587
11	.260	.697	1.363	1.796	2.201	2.718	3.106	3.497	4.025	4.437
12	.259	.695	1.356	1.782	2.179	2.681	3.055	3.428	3.930	4.318
13	.259	.694	1.350	1.771	2.160	2.650	3.012	3.372	3.852	4.221
14	.258	.692	1.345	1.761	2.145	2.624	2.977	3.326	3.787	4.140
15	0.258	0.691	1.341	1.753	2.131	2.602	2.947	3.286	3.733	4.073
16	.258	.690	1.337	1.746	2.120	2.583	2.921	3.252	3.686	4.015
17	.257	.689	1.333	1.740	2.110	2.567	2.898	3.222	3.646	3.965
18	.257	.688	1.330	1.734	2.101	2.552	2.878	3.197	3.610	3.922
19	.257	.688	1.328	1.729	2.093	2.539	2.861	3.174	3.579	3.883
20	0.257	0.687	1.325	1.725	2.086	2.528	2.845	3.153	3.552	3.850
21	.257	.686	1.323	1.721	2.080	2.518	2.831	3.135	3.527	3.819
22	.256	.686	1.321	1.717	2.074	2.508	2.819	3.119	3.505	3.792
23	.256	.685	1.319	1.714	2.069	2.500	2.807	3.104	3.485	3.767
24	.256	.685	1.318	1.711	2.064	2.492	2.797	3.091	3.467	3.745
25	0.256	0.684	1.316	1.708	2.060	2.485	2.787	3.078	3.450	3.725
26	.256	.684	1.315	1.706	2.056	2.479	2.779	3.067	3.435	3.707
27	.256	.684	1.314	1.703	2.052	2.473	2.771	3.057	3.421	3.690
28	.256	.683	1.313	1.701	2.048	2.467	2.763	3.047	3.408	3.674
29	.256	.683	1.311	1.699	2.045	2.462	2.756	3.038	3.396	3.659
30	0.256	0.683	1.310	1.697	2.042	2.457	2.750	3.030	3.385	3.646
40	.255	.681	1.303	1.684	2.021	2.423	2.704	2.971	3.307	3.551
60	.254	.679	1.296	1.671	2.000	2.390	2.660	2.915	3.232	3.460
120	.254	.677	1.289	1.658	1.980	2.358	2.617	2.860	3.160	3.373
$\infty$	.253	.674	1.282	1.645	1.960	2.326	2.576	2.807	3.090	3.291

Note: 1T = area under one tail; 2T = area under both tails.

For 25 degrees of freedom (d.f.),  $P(t > 2.060) = 0.025$  and  $P(t < -2.060 \text{ or } t > 2.060) = 0.05$ .Source: *Biometrika Tables for Statisticians*, Vol. I. Edited by E. S. Pearson and H. O. Hartley, 3rd edition, 1966.  
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**TABLE A.3** Upper Percentage Points of the Chi-Square Distribution  
( $v$  is the Degrees of Freedom and  $Q$  is the Area in the Right Tail)

$\nu \backslash Q$	0.250	0.100	0.050	0.025	0.010	0.005	0.001
1	1.32330	2.70554	3.84146	5.02389	6.63490	7.87944	10.828
2	2.77259	4.60517	5.99146	7.37776	9.21034	10.5966	13.816
3	4.10834	6.25139	7.81473	9.34840	11.3449	12.8382	16.266
4	5.38527	7.77944	9.48773	11.1433	13.2767	14.8603	18.467
5	6.62568	9.23636	11.0705	12.8325	15.0863	16.7496	20.515
6	7.84080	10.6446	12.5916	14.4494	16.8119	18.5476	22.458
7	9.03715	12.0170	14.0671	16.0128	18.4753	20.2777	24.322
8	10.2189	13.3616	15.5073	17.5345	20.0902	21.9550	26.125
9	11.3888	14.6837	16.9190	19.0228	21.6660	23.5894	27.877
10	12.5489	15.9872	18.3070	20.4832	23.2093	25.1882	29.588
11	13.7007	17.2750	19.6751	21.9200	24.7250	26.7568	31.264
12	14.8454	18.5493	21.0261	23.3367	26.2170	28.2995	32.909
13	15.9839	19.8119	22.3620	24.7356	27.6882	29.8195	34.528
14	17.1169	21.0641	23.6848	26.1189	29.1412	31.3194	36.123
15	18.2451	22.3071	24.9958	27.4884	30.5779	32.8013	37.697
16	19.3689	23.5418	26.2962	28.8454	31.9999	34.2672	39.252
17	20.4887	24.7690	28.5871	30.1910	33.4087	35.7185	40.790
18	21.6049	25.9894	28.8693	31.5264	34.8053	37.1565	42.312
19	22.7178	27.2036	30.1435	32.8523	36.1909	38.5823	43.820
20	23.8277	28.4120	31.4104	34.1696	37.5662	39.9968	45.315
21	24.9348	29.6151	32.6706	35.4789	38.9322	41.4011	46.797
22	26.0393	30.8133	33.9244	36.7807	40.2894	42.7957	48.268
23	27.1413	32.0069	35.1725	38.0756	41.6384	44.1813	49.728
24	28.2412	33.1962	36.4150	39.3641	42.9798	45.5585	51.179
25	29.3389	34.3816	37.6525	40.6465	44.3141	46.9279	52.618
26	30.4346	35.5632	38.8851	41.9232	45.6417	48.2899	54.052
27	31.5284	36.7412	40.1133	43.1945	46.9629	49.6449	55.476
28	32.6205	37.9159	41.3371	44.4608	48.2782	50.9934	56.892
29	33.7109	39.0875	42.5570	45.7223	49.5879	52.3356	58.301
30	34.7997	40.2560	43.7730	46.9792	50.8922	53.6720	59.703
40	45.6160	51.8051	55.7585	59.3417	63.6907	66.7660	73.402
50	56.3336	63.1671	67.5048	71.4202	76.1539	79.4900	86.661
60	66.9815	74.3970	79.0819	83.2977	88.3794	91.9517	99.607
70	77.5767	85.5270	90.5312	95.0232	100.425	104.215	112.317
80	88.1303	96.5782	101.879	106.629	112.329	116.321	124.839
90	98.6499	107.565	113.145	118.136	124.116	128.299	137.208
100	109.141	118.498	124.342	129.561	135.807	140.169	149.449
X	+0.6745	+1.2816	+1.6449	+1.9600	+2.3263	+2.5758	+3.0902

Note: For 25 d.f.,  $P(\chi^2 > 37.6525) = 0.05$ .

For  $v > 100$  take

$$\chi^2 = v \left\{ 1 - \frac{2}{9v} + X \sqrt{\frac{2}{9v}} \right\}^3 \quad \text{or} \quad \chi^2 = \frac{1}{3} \{ X + \sqrt{(2v-1)} \}^2,$$

according to the degree of accuracy required.  $X$  is the standardized normal deviate corresponding to  $P = 1 - Q$  and is shown in the bottom line of the table.

Source: Biometrika Tables for Statisticians, Vol. I. Edited by E. S. Pearson and H. O. Hartley, 3rd edition, 1966.  
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Upper 5% Points of the F-Distribution

$n \backslash m$	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	$\infty$
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5	241.9	243.9	245.9	248.0	249.1	250.1	251.1	252.2	253.3	254.3
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.41	19.43	19.45	19.46	19.47	19.48	19.49	19.50	19.50
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59	8.57	8.55	8.53
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46	4.43	4.40	4.36
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.77	3.74	3.70	3.67	3.67
7	5.69	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34	3.30	3.27	3.23
8	5.32	4.46	4.07	3.84	3.69	3.58	3.44	3.39	3.35	3.30	3.28	3.22	3.15	3.12	3.08	3.04	3.01	2.97	2.93
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83	2.79	2.75	2.71
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.74	2.70	2.66	2.62	2.58	2.54
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53	2.49	2.45	2.40
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.51	2.47	2.43	2.38	2.34	2.30
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34	2.30	2.25	2.21
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27	2.22	2.18	2.13
15	4.54	3.68	3.29	3.06	2.90	2.85	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20	2.16	2.07
16	4.49	3.63	3.24	3.01	2.95	2.74	2.66	2.61	2.55	2.49	2.44	2.38	2.35	2.30	2.28	2.24	2.19	2.15	2.07
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.11	2.06	2.01	1.96
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	2.21	2.15	2.11	2.06	2.02	1.97	1.92
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03	1.98	1.93	1.88
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99	1.95	1.90	1.84
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.92	1.87	1.81
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.37	2.32	2.27	2.20	2.13	2.07	2.03	1.98	1.94	1.89	1.84	1.78
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91	1.86	1.81	1.76
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89	1.84	1.79	1.73
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.82	1.77	1.71
26	4.23	3.37	2.98	2.75	2.59	2.47	2.39	2.32	2.27	2.22	2.16	2.07	1.99	1.95	1.90	1.85	1.80	1.76	1.69
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.06	1.97	1.93	1.88	1.84	1.79	1.73	1.67
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.77	1.71	1.65
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.03	1.94	1.90	1.85	1.81	1.75	1.70	1.64
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.03	1.98	1.93	1.89	1.84	1.79	1.74	1.62
40	4.08	3.23	2.84	2.61	2.46	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.69	1.64	1.58	1.51
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	2.02	1.99	1.92	1.84	1.75	1.70	1.65	1.59	1.47	1.39
120	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.61	1.55	1.50	1.43	1.35	1.25
$\infty$	3.84	3.00	2.60	2.37	2.21	2.10	1.94	1.88	1.83	1.76	1.67	1.57	1.52	1.46	1.39	1.32	1.22	1.00	

Note:  $m$  = degrees of freedom for the numerator $n$  = degrees of freedom for the denominatorSource: *Handbook of Tables for Mathematics*, edited by Robert C. West and Samuel M. Selby, 1970. Reprinted with the permission of the CRC Press, Inc.